

Q2. $X =$ lifetime of component.

$X \sim \text{exp}(\lambda)$.

$$\begin{aligned} p &= P(X \geq 24) = 1 - P(X \leq 24) \\ &= 1 - F(24; \lambda) \\ &= 1 - (1 - e^{-24\lambda}) \\ &= e^{-24\lambda}. \end{aligned}$$

$Y =$ number that survive 24h

$Y \sim \text{binomial}(n, p)$

$$\hat{p} = \frac{y}{n} = \frac{15}{18} \quad (y=15, n=18)$$

by invariance principle

$$\implies \hat{p} = e^{-24\lambda}$$

$$\implies \hat{\lambda} = -\frac{\ln \hat{p}}{24}$$